

HW 4 - FIT EQN TO DATA

e.g., $r_{\text{MODEL}} = f(a_1, a_2, P_1, P_2)$ WHERE a_1, a_2 ARE UNKNOWN SCALARS (ONE VALUE)
 P_1, P_2 ARE KNOWN ARRAYS OF EXP'L VALUES

GOAL FIND VALUES OF a_1, a_2 THAT

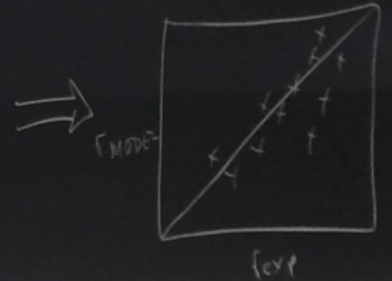
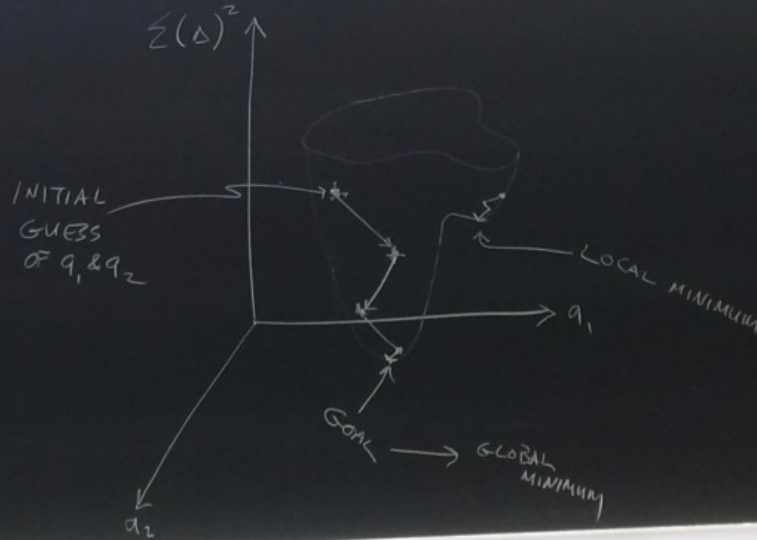
OR OTHER
"OBJECTIVE
FUNCTION"

$$\text{e.g. } \sum \left(\frac{r_{\text{EXP}} - r_{\text{MODEL}}}{r_{\text{EXP}}} \right)^2$$

MINIMIZE $\sum (r_{\text{EXP}} - r_{\text{MODEL}})^2 = \text{SUM OF SQUARED ERRORS} \Rightarrow$

USE SOFTWARE THAT
DOES THIS

fminsearch IN MATLAB
Solver IN EXCEL
OR YOUR CHOICE



LAST TIME - 1ST ORDER, "IRREV" RXN IN POROUS SLAB CATALYST \Rightarrow eg, $r_A = \frac{-kC_A}{1+K_A C_A}$ @ RELATIVELY LOW C SUCH THAT $r \rightarrow -kC_A$

$\frac{d^2\psi}{dx^2} - \phi^2\psi = 0$ B.C. 1) $e^{-\lambda} = 0 \quad \frac{d\psi}{dx} = 0$
 $e^{-\lambda} = 1 \quad \psi = 1$

$\phi = \text{THIELE MODULUS} = R(m) \sqrt{\frac{k(C_{A,s})}{D_{eff}(m^2/s)}}$

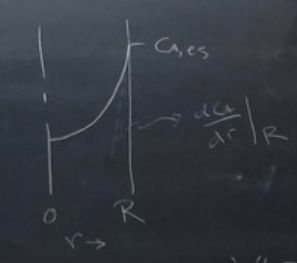
$\phi^2 = \frac{R k C_{A,s}}{D_{eff} \left(\frac{C_{A,s}}{R}\right)} = \frac{\text{RATE IF ALL SITES SEE } C_{A,s} \text{ (NEGL DIFF RESIST)}}{\text{DIFF. RATE WITH NO RXN \& CENTER CONC} = 0}$
 (MAX DIFF RATE WITH NO RXN)

$\psi(\lambda) = \frac{\cosh(\phi\lambda)}{\cosh\phi}$ where $\cosh x = \frac{e^x + e^{-x}}{2}$

$C_A(r)$ \downarrow
 \uparrow HYPERBOLIC COSINE

WANT AVE RATE OVER CATALYST LAYER \rightarrow (1) INTEGRATE $r_T C_A(r)$ OVER r & AVERAGE

(2) GET $\frac{dC_A}{dr} \Big|_{r=R}$ OR $\frac{d\psi}{d\lambda} \Big|_{\lambda=1}$ & GET AVE. RATE FROM THIS



NET RATE "A" DIFFUSES INTO LAYER

$= A_r (m^2) D_{eff} \left(\frac{m^2}{s}\right) \frac{dC_A}{dr} \left(\frac{mol}{m^3 \cdot m}\right)$

$$\left. \frac{d\psi}{d\lambda} \right|_{\lambda=1} = \phi^2 \left(\frac{\tanh \phi}{\phi} \right) = \phi \tanh \phi$$

HYPERBOLIC TANGENT. $\rightarrow \tanh x = \frac{e^x - e^{-x}}{e^x + e^{-x}}$

WE KNOW
 $-r_{A, \text{TRUE}} = k_T C_A$
 WE WANT \rightarrow

$$-r_{A, \text{OBS}} = k_{\text{OBS}} C_{A, \text{es}}$$

$$k_{\text{OBS}} = k_{\text{OBSERVED WITH DIFFUSION RESISTANCE}} \neq k_{\text{TRUE}}$$

WHEN SIGNIFICANT
 DIFFUSION RESISTANCE
 IS PRESENT

$$-r_{A, \text{OBS}} = \eta k_{\text{TRUE}} C_{A, \text{es}}$$

RATE WITH NEGLIGIBLE DIFF RESIST.

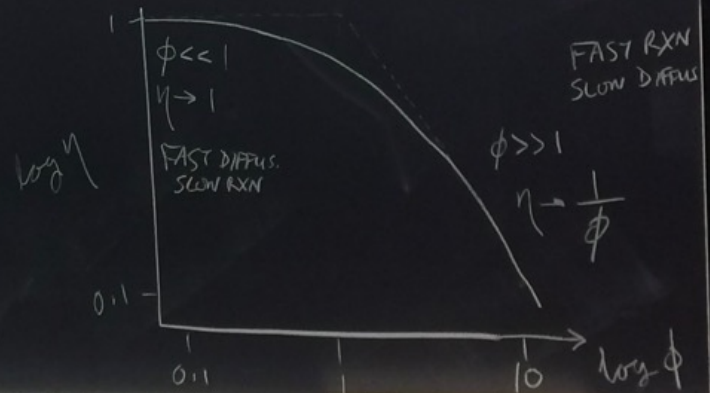
RATE WITH SIGNIFIC
 DIFF. RESIST.

$$\therefore \eta = \frac{\text{RATE WITH DIFFUSION RESISTANCE}}{\text{RATE WITH NO DIFF. RESIST.}}$$

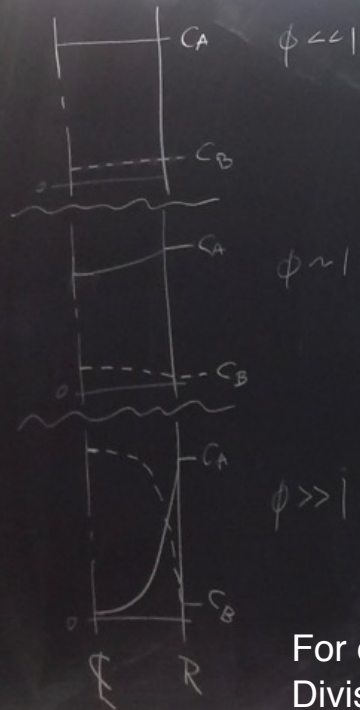
"INTERNAL EFFECTIVENESS FACTOR" (GREEK "ETA")

FOR THIS CASE \rightarrow "IRREV" 1st ORDER, A \rightarrow B, ISOTHERMAL

$$\eta = \frac{\tanh \phi}{\phi}$$



DRAW CONC. PROFILES A → B



LOOK @ UNITS

$$R \left(\frac{1}{s} \right) = k' \left(\frac{m^3}{kg \cdot s} \right) \underbrace{\rho_{\text{PELLET}} \left(\frac{kg}{m^3} \right)}_{\text{PELLET DENSITY}} = k'' \left(\frac{m}{s} \right) \underbrace{S_a \left(\frac{m^2}{kg} \right) \rho_P \left(\frac{kg}{m^3} \right)}_{\text{ACTIVE SITE AREA PER UNIT MASS}}$$

$$\phi = R(m) \sqrt{\frac{R(1/s)}{D_{eff}(m^2/s)}} = R \sqrt{\frac{k' S_a \rho_P}{D_{eff}}}$$

$$-r_{A, \text{TRUE}} \left(\frac{\text{mol}}{m^2 \cdot s} \right) = k' (1/s) C_A \left(\frac{\text{mol}}{m^3} \right)$$

↑ OF CATALYST
↑ OF FLUID

$$-r_{A, \text{TRUE}} \left(\frac{\text{mol}}{kg \cdot s} \right) = k' \left(\frac{m^3}{kg \cdot s} \right) C_A \left(\frac{\text{mol}}{m^3} \right)$$

For concentration profiles, see Reactor Lab program, Division 2, Lab 1, and also Division 7, Labs 2 and 3